

Learning Grammatical Constructions

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Abstract

We describe a computational model of the acquisition of early grammatical constructions that exploits two essential features of the human language learner: significant prior knowledge of concepts and individual lexical items, and sensitivity to the statistical properties of the input data. Such principles, previously applied to lexical acquisition, are shown to be useful and necessary for learning the structured mappings between form and meaning needed to represent phrasal and clausal constructions. We describe an algorithm based on Bayesian model merging that can induce a set of grammatical constructions based on simpler previously learned constructions in combination with new utterance-situation pairs. The resulting model shows how cognitive and computational constraints can intersect to produce a course of learning consistent with data from studies of child language acquisition.

Introduction

We describe a computational model of the acquisition of early grammatical constructions that exploits two essential features of the human language learner: significant prior knowledge of both concepts and individual lexical items, and sensitivity to the statistical properties of the input data. Precocity on both fronts is usually assumed to be crucial for lexical acquisition, as exemplified by some proposed models for learning spatial relations terms (Regier, 1996), object labels (Roy and Pentland, 1998) and action labels (Bailey, 1997; Siskind, 1997). We focus here on larger phrasal and clausal constructions and investigate the extent to which they can be learned using the same principles employed in word learning.

We take as both inspiration and constraint the course of development observed in crosslinguistic studies of child language acquisition. In particular, our present domain of inquiry is restricted to the shift from single words to word combinations, and our model makes strong assumptions about prior knowledge – both ontological and linguistic – on the part of the learner.

After describing these assumptions, we address the representational complexities associated with larger grammatical constructions. In the framework of Construction Grammar (Goldberg, 1995), these constructions can, like single-word constructions, be viewed as mappings between the two domains of *form* and *meaning*, where form typically refers to the speech or text

stream and meaning refers to a rich conceptual ontology. They may also, however, involve relations among multiple entities in both form (e.g., multiple words and/or phonological units) and meaning (multiple participants in a scene). We introduce a simple formalism capable of representing such relational constraints.

The remainder of the paper casts the learning problem in terms of two interacting processes, construction hypothesis and construction reorganization, and presents an algorithm based on Bayesian model merging for inducing the best set of constructions to fit previously seen data and generalize to new data. We conclude by discussing some of the broader implications of the model for language learning and use.

Prerequisites

Our model of grammar learning makes several crucial assumptions that acknowledge the significant prior knowledge the language learner brings to the task. These fall into two broad categories: representational requirements for ontological knowledge; and the ability to acquire lexical mappings.

Conceptual Representations

Infants inhabit a dynamic world of continuous percepts, and how they process and represent these fluid sensations remains poorly understood. Well before the first recognizable words are produced, however, a substantial repertoire of concepts corresponding to people, objects, settings and actions will have emerged from the chaos as the beginnings of a stable ontology.

The acquisition of these concepts from naturalistic input has been addressed by models in probabilistic, connectionist, clustering and logical frameworks.¹ For our current spotlight on the acquisition of grammatical structures, we require only that conceptual representations exhibit the kinds of category and similarity effects known to be pervasive in human cognition (Lakoff, 1987). That is, concepts should cluster into categories with prototype structure and graded category membership. Representations should also facilitate the identification of similar

¹Typically, input data corresponding to sensorimotor input is described using a set of continuous and/or discrete features, and standard machine learning techniques are used to acquire categories based on supervised or unsupervised training.

concepts and provide some basis for generalization. The current model uses an inheritance hierarchy with concepts represented as feature structures.

An important additional requirement comes from the assumption that many early concepts involve multiple entities interacting within the context of some unified event (Tomasello, 1992) or *frame*. Prelinguistic children are competent event participants who have accumulated structured knowledge about the roles involved in different events and the kinds of entities likely to fill them. Frame-based representations can capture the crucial relational structure of many concepts, including not only early sensorimotor knowledge but also aspects of the surrounding social and cultural context.

It will be convenient to represent frames in terms of individual role bindings: *Throw.thrower:Human* and *Throw.throwee:Object* together bind a *Throw* frame with a *Human* thrower acting on an *Object* throwee. Note that although this representation highlights relational structure and obscures lower-level features of the underlying concepts, both aspects of conceptual knowledge will be crucial to our approach to language learning.

Lexical Mappings

Lexical mappings associate an acoustic signal with an arbitrary concept, ranging from familiar people and objects to much more complex actions and interactions whose physical referents may be more transient and difficult to identify. Lexical items are initially tightly coupled with the specific events, contexts and even purposes with which they have co-occurred. Words are also subject to polysemy effects, since the same form may be encountered in multiple distinct (though possibly related) contexts, which may be diverse enough to resist a single generalization. The word *up*, for example, may initially have several distinct uses: as a request to be picked up; as a comment on an upward movement; and as a remark about a highly placed item.

It is important to note that word learning involves much more than simply associating sound and meaning. As described in detail by Bloom (2000), sophisticated means of determining referential intent must be employed to form the appropriate lexical mappings, and general pragmatic skills must play a dominant role in helping the child make sense of her environment, especially before she has amassed a collection of stable form-meaning pairs. We do not attempt to model these complex reasoning skills, which are necessary for successful behavior in general and are not specific to the learning task at hand.

But regardless of the complexity of either the referent or the process by which it is inferred, the resulting map is relatively simple: a given form can be mapped to a single concept, or to several (possibly differentially weighted) concepts. Our initial set of constructions contains a number of such lexical form-meaning maps, where for simplicity we further constrain these to be mappings from orthographic forms to feature-structure meanings, as in Bailey (1997).

We now turn to the representationally more complex case of grammatical constructions, before addressing how such constructions are learned.

Grammatical Constructions

We base our representations of grammatical knowledge on ideas from Construction Grammar (Goldberg, 1995) and Cognitive Grammar (Langacker, 1991). In these approaches, larger phrasal and clausal units are, like lexical constructions, pairings of form and meaning. A key observation in the Construction Grammar tradition is that the meaning of a sentence may not be strictly predictable from the meaning of its parts; the syntactic pattern itself may also contribute a particular conceptual framing. For example, the *CAUSED-MOTION* construction underlying *Pat sneezed the napkin off the table* imposes a causative reading on the typically non-causative verb *sneeze*, and the need for an agentive recipient in the *DI-TRANSITIVE* construction renders *Harry kicked the door the ball* somewhat anomalous.

On this account, syntactic patterns are inextricably linked with meaning, and grammaticality judgments are rightly influenced by semantic and pragmatic factors. The interpretation and acceptability of an utterance thus depends not only on well-formedness conditions but also on the structure of the language user's conceptual ontology and on the situational and discourse context.

The main representational complexity introduced with these multiword constructions is the possibility of structure in the form pole. As mentioned, although individual lexical items can evoke complex frames with multiple participant roles (e.g., *bye-bye*, *baseball*), the actual mapping between the form and meaning pole is necessarily straightforward. With multiple form units available, however, additional structures arise, both within the form pole itself and, more significantly, in the *relational correlations* between the form and meaning poles.² That is, a multiword construction may involve a more complex, *structured map* between its form and meaning poles, with maps between form and meaning relations whose arguments are also mapped.

In addition to the sound patterns of individual words, the form pole includes intonational contours, morphological inflections and word order. As with single words, the meaning pole encompasses the much larger set of frame-based conceptual knowledge. The constructional mapping between the two domains typically consists of a set of form relations (such as word order) corresponding to a set of meaning relations (such as a role-filler binding). As an example, Figure 1 gives an iconic representation of some of the possible constructions involved in an analysis of *I throw the ball*. The lexical constructions for *I*, *THROW* and *THE-BALL*³ all have simple poles of both form and meaning. But besides the individual words and

²See Gasser and Colunga (2000) for arguments that the ability to represent relational correlations underlies infants' reputed aptitude for statistically driven learning of concrete and abstract patterns.

³The definite determiner *the* explicitly depends on a repre-

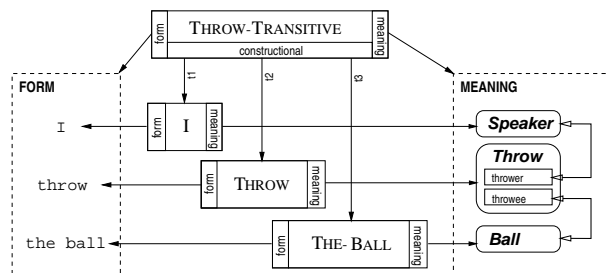


Figure 1: A constructional analysis of the sentence, *I throw the ball*, with form elements at left, meaning elements at right and some constituent constructions linking the two domains in the center.

concepts involved in the utterance, we have several word order relationships (not explicitly represented in the diagram) that can be detected in the form domain, and bindings between the roles associated with *Throw* and other semantic entities (as denoted by the double-headed arrows within the meaning domain). Finally, the larger clausal construction (in this case, a verb-specific one) has constituent constructions, each of which is filled by a different lexical construction.⁴ Crucially, the clausal construction serves to associate the specified form relations with the specified meaning relations, where the arguments of these relations are already linked by existing (lexical) maps.

A more formal representation of the **THROW-TRANSITIVE** construction is given in Figure 2. For current purposes, it is sufficient to note that this representation captures the constituent constructions, as well as constraints on its formal, semantic and constructional elements. Each constituent has an alias used locally to refer to it, and subscripts f and m are used to denote the constituent's form and meaning poles, respectively. A designation constraint specifies a meaning type for the overall construction.

Although this brief discussion necessarily fails to do justice to Construction Grammar and related work, we hope that it nevertheless conveys the essential representational demands on the structures to be learned.

Learning Constructions

We can now specify our construction learning task: Given an initial set of constructions \mathcal{C} and a sequence of new training examples, find the best set of constructions \mathcal{C}' to fit the seen data and generalize to new data. In accord with our discussion of conceptual prerequisites, a training example is taken to consist of an utterance paired with a representation of a situation, where the former is a sequence of familiar and novel forms, and the latter a

sentation of the situational and discourse context that supports reference resolution. For simplicity, we will ignore the internal structure of “the ball” and treat it as an unstructured unit.

⁴This example, like the rest of those in the paper, is based on utterances from the CHILDES corpus (MacWhinney, 1991) of child-language interaction.

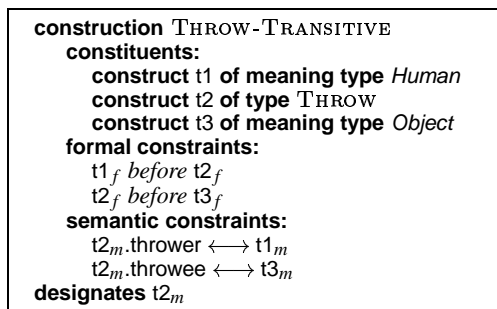


Figure 2: Formal representation of the **THROW-TRANSITIVE** construction, with separate blocks listing constituent constructions, formal constraints (e.g., word order) and semantic constraints (role bindings).

set of frame-based conceptual entities and role bindings representing the corresponding scene.

Previous work on Bayesian model merging (Stolcke, 1994; Bailey, 1997) provides a suitable starting point. In that framework, training data is first incorporated, with each example stored as an independent model. Then similar models are merged (and generalized); the resulting drop in likelihood is balanced against an increase in the prior, which is based on minimum description length. Merging continues until the posterior probability of the model decreases.

A similar strategy can be applied to our current task, which can be cast as a search through the space of possible grammars (or sets of constructions), where these grammars can be evaluated using Bayesian criteria. The operations on the set of constructions (merging and composition, described below as **reorganization** processes) are straightforward extensions of operations used in previous work, though they must be modified to handle relational structures. Similarly, the evaluation criteria need not change significantly for the construction learning case. Specifically, a prior based on minimum description length favors grammars with fewer, more general constructions that compactly encodes previously seen data; this measure combats the inevitable corresponding drop in likelihood. As usual, the learning algorithm chooses the set of constructions that maximizes the posterior probability of the set of constructions given the data.

The main complication requiring a departure from previous work is the need to hypothesize structured maps between form and meaning like those described in the previous section. Essentially, incorporating new data involves both the **analysis** of an utterance according to known constructions and the **hypothesis** of a new construction to account for any new mappings present in the data. These processes, described below, are based on the assumption that the learner expects correlations between what is heard (the utterance) and what is perceived (the situation).⁵ Some of these correlations have

⁵The task as defined here casts the learner as primarily comprehending (and not producing) grammatical utterances. Note,

already been encoded and thus accounted for by previously learned constructions; the tendency to try to account for the remaining ones leads to the formation of new constructions. In other words, what is learned depends directly on what remains to be explained. The identification of the mappings between an utterance and a situation that are predicted by known constructions can be seen as a precursor to language comprehension, in which the same mappings actively evoke meanings not present in the situation. Both require the learner to have an analysis procedure that determines which constructions are potentially relevant, given the utterance, and, by checking their constraints in context, finds the best-fitting subset of those.

Once the predictable mappings have been explained away, the learner must have a procedure for determining which new mappings may best account for new data. The mappings we target here are, as described in the previous section, relational. It is crucial to note that a relational mapping must hold across arguments that are themselves *constructionally correlated*. That is, mappings between arguments must be in place before higher-order mappings can be acquired. Thus the primary candidates for relational mappings will be relations over elements whose form-meaning mapping has already been established. This requirement may also be viewed as narrowing the search space to those relations that are deemed *relevant* to the current situation, as indicated by their connection to already recognized forms and their mapped meanings.

Details of these procedures are best illustrated by example. Consider the utterance $U_1 = \text{“you throw a ball”}$ spoken to a child throwing a ball. The situation S consists of entities S_e and relations S_r ; the latter includes role bindings between pairs of entities, as well as attributes of individual entities. In this case, S_e includes the child, the thrown ball and the throwing action, as well as potentially many other entities, such as other objects in the immediate context or the parent making the statement: $S_e = \{\text{Self, Ball, Block, Throw, Mother, ...}\}$. Relational bindings include those encoded by the Throw frame, as well as other properties and relations: $S_r = \{\text{Throw.thrower:Self, Throw.throwee:Ball, Ball.Color:Yellow, ...}\}$.

In the following sections we describe what the learner might do upon encountering this example, given an existing set of constructions C that has lexical entries for BALL, THROW, BLOCK, YOU, SHE, etc., as well as a two-word THROW-BALL construction associating the `before(throw,ball)` word-order constraint with the binding of Ball to the throwee role of the Throw frame.

Construction analysis and hypothesis

Given this information, the analysis algorithm in Figure 3 first extracts the set $F_{known} = \{\text{you, throw, ball}\}$,

however, that the learning algorithm is broadly compatible with allowing production-based means of hypothesizing new mappings, which would be included in a more complete model.

which serves to cue constructions that have any of these units in the form pole. In this case, $C_{cued} = \{\text{YOU, THROW, BALL, THROW-BALL}\}$. Next, the constraints specified by these constructions must be matched against the input utterance and situation. The form constraints for all the lexical constructions are trivially satisfied, and in this case each also happens to map to a meaning element present in S .⁶ Checking the form and meaning constraints of the THROW-BALL construction is also trivial: all relations of interest are directly available in the input utterance and situation.⁷

Analyze utterance. Given utterance U in situation S and current constructions C , produce best-fitting analysis A :

1. Extract the set F_{known} of familiar form units from U , and use them to cue the set C_{cued} of constructions.
2. Find the best-fit analysis $A = \langle C_A, F_A, M_A \rangle$, where C_A is the best-fitting subset of C_{cued} for utterance U in situation S , F_A is the set of form units and relations in U used in C_A , and M_A is the set of meaning elements and bindings in S accounted for by C_A .
 A has associated cost $Cost_A$ providing a quantitative measure of how well A accounts for U in S .
3. Reward constructions in C_A ; penalize cued but unused constructions, i.e., those in $C_{cued} \setminus C_A$.

Figure 3: Construction analysis.

In the eventual best-fitting analysis A , the constructions used are $C_A = \{\text{YOU, THROW, BALL, THROW-BALL}\}$, which cover the forms and form relations in $F_A = \{\text{you, throw, ball, before(throw, ball)}\}$ and map the meanings and meaning relations in $M_A = \{\text{Self, Throw, Ball, Throw.throwee:Ball}\}$. (Remaining unused in this analysis is the form a.)

We proceed with our example by applying the procedure shown in Figure 4 to hypothesize a new construction. All form relations and meaning bindings, respectively, that are *relevant* to the form and meaning entities involved in the analysis are extracted as, respectively, $F_{rel} = \{\text{before(you, throw), before(throw, ball), before(you, ball)}\}$ and $M_{rel} = \{\text{Throw.thrower:Self, Throw.throwee:Ball}\}$; the *remainder* of these not used in the analysis are $F_{rem} = \{\text{before(you, throw), before(you, ball)}\}$ and $M_{rem} = \{\text{Throw.thrower:Self}\}$. The potential construction C_{pot} derived by replacing terms with constructional references is made up of form pole $\{\text{before(YOU}_f, \text{THROW}_f), \text{before(YOU}_f, \text{BALL}_f)\}$

⁶We assume the YOU construction is a context-dependent construction that in this situation maps to the child (Self).

⁷Many complications arise in adult language – category constraints on roles may apply only weakly, or may be overridden by the use of metaphor or context. At the stage of interest here, however, we assume that all constraints are simple and few enough that exhaustive search should suffice, so we omit the details about how cueing constructions, checking constraints and finding the best-fitting analysis proceed.

and meaning pole $\{\text{THROW}_m.\text{thrower:YOU}_m\}$. The final construction C_{U_1} is obtained by retaining only those relations in C_{pot} that hold over correlated arguments:

$(\{\text{before}(\text{YOU}_f, \text{THROW}_f)\}, \{\text{THROW}_m.\text{thrower:YOU}_m\})$

Hypothesize construction. Given analysis A of utterance U in situation S , hypothesize new construction C_U linking correlated but unused form and meaning relations:

1. Find the set F_{rel} of form relations in U that hold between the familiar forms F_{known} , and the set M_{rel} of meaning relations in S that hold between the mapped meaning elements in M_A .
2. Find the set $F_{rem} = F_{rel} \setminus F_A$ of relevant form relations that remain unused in A , and the set $M_{rem} = M_{rel} \setminus M_A$ of relevant meaning relations that remain unmapped in A . Create a potential construction $C_{pot} = (F_{rem}.M_{rem})$, replacing terms with references to constructions in C_A where possible.
3. Create a new construction C_U consisting of pairs of form-meaning relations from C_{pot} whose arguments are constructionally related.
4. Reanalyze utterance using $C \cup \{C_U\}$, producing a new analysis A' with cost $Cost_{A'}$. Incorporate C_U into C if $Cost_A - Cost_{A'} \geq \text{MinImprovement}$; else put C_U in pool of potential constructions.
5. If U contains any unknown form units, add the utterance-situation pair (U, S) to the pool of unexplained data.

Figure 4: Construction hypothesis.

At this point, the utility of C_{U_1} can be evaluated by reanalyzing the utterance to ensure a minimum reduction of the cost of the analysis. As noted in Step 4 of Figure 4, a construction not meeting this criterion is held back from immediate incorporation into C . It is possible, however, that further examples will render it useful, so it is maintained as a candidate construction. Similarly, Step 5 is concerned with maintaining a pool of examples that involve unexplained units of form, such as the unfamiliar article a in this example. Further examples involving similar units may together lead to the correct generalization, through the reorganization process to which we now turn.

Reorganizing constructions

The analysis-hypothesis process just described provides the basis for incorporating new examples into the set of constructions. A separate process that takes place in parallel is the data-driven, bottom-up reorganization of the set of constructions on the basis of similarities among and co-occurrences of multiple constructions. Figure 5 gives a high-level description of this process; we refrain from delving into too much detail here, since these processes are closely related to those described for other generalization problems (Stolcke, 1994; Bailey, 1997).

Continuing our example, let us assume that the utterance $U_2 = \text{“she’s throwing a frisbee”}$ is later encountered

Reorganize constructions. Incorporate new construction C_n into an existing set of constructions C , reorganizing C to consolidate similar and co-occurring constructions:

1. Find potential construction pairs to consolidate.
 - **Merge** constructions involving correlated relational mappings over one or more pairs of similar constituents, basing similarity judgments and type generalizations on the conceptual ontology.
 - **Compose** frequently co-occurring constructions with compatible constraints.
2. Evaluate constructions; choose the subset maximizing the posterior probability of C on seen data.

Figure 5: Construction reorganization.

in conjunction with an appropriate scene, with similar results: in this case, both the unfamiliar inflections and the article are ignored; the meanings are mapped; and constraints with appropriate correlations are found, resulting in the hypothesis of the construction C_{U_2} :

$(\{\text{before}(\text{SHE}_f, \text{THROW}_f)\}, \{\text{THROW}_m.\text{thrower:SHE}_m\})$

C_{U_1} and C_{U_2} bear some obvious similarities: both constructions involve the same form relations and meaning bindings, which hold of the same constituent construction **THROW**. Moreover, the other constituent is filled in the two cases by **SHE** and **YOU**. As emphasized in our discussion of conceptual representations, a key requirement is that the meaning poles of these two constructions reflect their high degree of similarity.⁸ The overall similarity between the two constructions can lead to a merge of the constructional constituents, resulting in the merged construction:

$(\{\text{before}(\mathbf{h}_f, \text{THROW}_f)\}, \{\text{THROW}_m.\text{thrower:h}_m\})$

where \mathbf{h} is a variable over a construction constrained to have a *Human* meaning pole (where *Human* is a generalization over the two merged constituents). A similar process, given appropriate data, could produce the generalized mapping:

$(\{\text{before}(\text{THROW}_f, \mathbf{o}_f)\}, \{\text{THROW}_m.\text{throwee:o}_m\})$

where \mathbf{o} is constrained to have an *Object* meaning pole.⁹

Besides merging based on similarity, constructions may also be composed based on co-occurrence. For example, the generalized *Human-THROW* and *THROW-Object* constructions just described are likely to occur in many analyses in which they share the **THROW** constituent. Since they have compatible constraints in both form and meaning (in the latter case even based on the

⁸The precise manner by which this is indicated is not at issue. For instance, a type hierarchy could measure the distance between the two concepts, while a feature-based representation might look for common featural descriptions.

⁹Although not further discussed here, examples with unexplained forms (such as the a in U_1 and U_2) may also undergo merging, leading to the emergence of common meanings.

same conceptual Throw frame), repeated co-occurrence eventually leads to the formation of a larger construction that includes all three constituents:

$$(\{\text{before}(\mathbf{h}_f, \text{THROW}_f), \text{before}(\text{THROW}_f, \mathbf{o}_f)\}, \\ \{\text{THROW}_m.\text{thrower}:\mathbf{h}_m, \text{THROW}_m.\text{throwee}:\mathbf{o}_m\})$$

Note that both generalization operations we describe are, like the hypothesis procedure, merely means of finding potential constructions, and are subject to the evaluation criteria mentioned earlier.

Discussion

The model we have proposed for the acquisition of grammatical constructions makes some claims about the relationship between comprehension and learning. We take these processes to be tightly linked: new constructions are hypothesized specifically to make up for correlations not covered by currently known constructions. As noted, a more complete model would include more active production-based means of hypothesizing constructions as well.

The model is compatible to the extent possible with evidence from child language acquisition. The principles guiding construction hypothesis, in particular those for mapping relevant form and meaning relations, have counterparts in some of Slobin's (1985) Operating Principles for mapping. Construction reorganization allows more general constructions to result from the merging of lexically specific constructions like those described by (Tomasello, 1992).

More broadly, since the algorithm produces constructions based on any utterance-situation pair and existing set of constructions represented as described above, it can apply equally well for more advanced stages of language development, when the learner has more sophisticated meaning representations and more complex constructions. The potential continuity between early language acquisition and lifelong constructional reorganization offers hope for the modeling of adaptive language understanding systems, human and otherwise.

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